

Surface areas and volumes

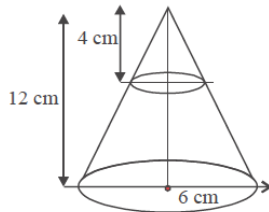
1 Mark

1. A solid shape is converted from one form of another. What is the change in its volume?
2. What cross-section is made by a cone when it is cut parallel to its base?
3. Find total surface area of a solid hemi-sphere of radius 7cm.
4. Volume of two spheres is in the ratio 64 : 125. Find the ratio of their surface areas.
5. A right circular cylinder of radius r cm and height h cm ($h > 2r$) just encloses a sphere. Find diameter of the sphere.
6. A cylinder and a cone are of same base radius and of same height. Find the ratio of the volumes of cylinder to that of the cone.
7. A solid sphere of radius r is melted and recast into the shape of a solid cone of height r . Find radius of the base of the cone.
8. Find the total surface area of a solid hemi-sphere of radius r .
9. If the volume and the surface area of a sphere are numerically equal, then find the radius of the sphere.
10. A cylinder, a cone and a hemisphere are of same base and have the same height. What is the ratio of their volumes?
11. If two solid hemi-spheres of same base radius r are joined together along their base, then find the total surface area of this new solid.
12. If the volume of a cube is 1331 cm^3 , then find the length of its edge.
13. What does the "CAPACITY" for a hollow cylinder means?

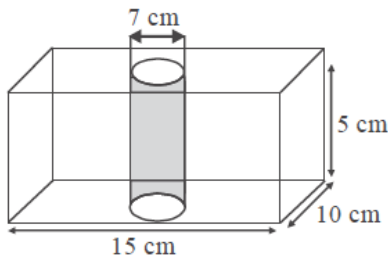
2/3/4 Marks

14. How many cubes of side 2 cm can be cut from a cuboid measuring $(16\text{cm} \times 12\text{cm} \times 10\text{cm})$.
15. Find the height of largest right circular cone that can be cut out of a cube whose volume is 729 cm^3 .
16. Two identical cubes each of volume 64 cm^3 are joined together end to end. What is the surface area of the resulting cuboid?
17. Twelve solid spheres of the same sizes are made by melting a solid metallic cylinder of base diameter 2 cm and height 16cm. Find the radius of each sphere.
18. The diameters of the two circular ends of the bucket are 44 cm and 24 cm. The height of the bucket is 35cm. Find the volume of the bucket.
19. Find the length of the longest rod that can be put in a room of $10\text{m} \times 10\text{m} \times 5\text{m}$ dimensions.
20. Find surface area of a cube whose volume is 1000 cm^3 .
21. The volume of two hemi-sphere are in the ratio 8:27. Find the ratio of their radii.
22. Find the curved surface area and the total surface area of a solid cone whose height is 28 cm and radius is 21 cm.
23. A bucket is in the form of a frustum of a cone and hold a 28.490 liters of water. The radii of the top and bottom are 28 cm and 21 cm respectively. Find the height of the bucket.
24. Three cubes of a metal whose edge are in the ratio 3:4:5 are melted and converted into a single cube whose diagonal is $12\sqrt{3}\text{cm}$. Find the edge of three cubes.
25. Find the depth of a cylindrical tank of radius 10.5 cm, if its capacity is equal to that of a rectangular tank of size $15 \text{ cm} \times 11 \text{ cm} \times 10.5 \text{ cm}$.
26. A cone of radius 8cm and height 12cm is divided into two parts by a plane through the mid-point of its axis parallel to its base. Find the ratio of the volumes of the two parts.

27. A petrol tank is a cylinder of base diameter 28cm and length 24cm filled with conical ends each of axis length 9cm. Determine the capacity of the tank.
28. In the given figure, from the top of a solid cone of height 12cm and base radius 6cm, a cone of height 4 cm is removed by a plane parallel to the base. Find the total surface area of the remaining solid. $(\pi = \frac{22}{7}, \sqrt{5} = 2.236)$



29. A solid wooden toy is in the form of a hemi-sphere surmounted by a cone of same radius. The radius of hemi-sphere is 3.5cm and the total wood used in the making of toy is $166\frac{5}{6} \text{ cm}^3$. Find the height of the toy. Also, find the cost of painting the hemi-spherical part of the toy at the rate of Rs. 10 per cm^2 . $(\pi = \frac{22}{7})$
30. In the given figure, from a cuboidal solid metallic block of dimensions 15 cm \times 10 cm \times 5 cm a cylindrical hole of diameter 7cm is drilled out. Find the surface area of the remaining block. $(\pi = \frac{22}{7})$



31. Water is flowing at the rate of 2.52 km/hr. through a cylindrical pipe into a cylindrical tank, the radius of whose base is 40 cm. If the increase in the level of water in the tank, in half an hour is 3.15m, find internal diameter of the pipe.
32. A solid toy is the form of a right circular cylinder with a hemispherical shape at one end and a cone at the other end. Their diameter is 4.2 cm and the heights of the cylindrical and conical portions are 12 cm and 7 cm respectively. Find the volume of the toy.
33. A tent is in the shape of a right circular cylinder upto a height of 3m and conical above it. The total height of the tent is 13.5 m and radius of base is 14 m. Find the cost of cloth required to make the tent at the rate of Rs. 80 per sq. m.
34. The rain water from a roof 22m \times 20m drains into a cylindrical vessel having diameter of base 2m and height 3.5m. If the vessel is just full, find the rainfall in cm.
35. A container, shaped like a right circular cylinder, having diameter 12cm and height 15 cm is full of ice-cream. this ice-cream is to be filled into cones of height 12 cm and diameter 6 cm, having a hemispherical shape on the top. Find the number of such cones which can be filled with ice-cream.
36. The difference between outer and inner curved surface areas of a hollow right circular cylinder, 14 cm long is 88 cm^2 . If the volume of the metal used in making the cylinder is 176 cm^3 . Find the outer and inner diameters of the cylinder.
37. A toy is in the shape of a right circular cylinder with a hemisphere on one end and a cone on the other. The radius and height of the cylindrical part are 5 cm and 13 cm

respectively. The radii of hemispherical and parts are the same as that of the cylindrical part. Find the surface area of the toy if the total height of the toy is 30 cm.

38. A hollow cone is cut by a plane parallel to the base and the upper portion is removed. If the curved surface of the remainder is $\frac{8}{9}$ th of the curved surface of the whole cone, find the ratio of the line segments into which the altitude of the cone is divided by the plane.

Answers

1 Mark

1. Remains Uncharged
2. Circle
3. 462 cm^2
4. 16:25
5. $2r$
6. 3:1
7. $2r$
8. $3\pi r^2$
9. 3 units
10. 3:1:2
11. $4\pi r^2$
12. 11 cm^2
13. Volume

2/3/4 Marks

14. 240
15. 9 cm
16. 160 cm^2
17. 1 cm
18. 32706.6 cm^3

19. 15 m
20. 600 cm^2
21. 2:3
22. C.S.A = 2310 cm^2 , T.S.A = 3696 cm^2
23. 15 cm
24. 6 cm, 8 cm, 10 cm
25. 5 cm
26. 1:7 or 7:1
27. 18480 cm^3
28. 350.592 cm^2
29. H = 6 cm, Rs. 770
30. 583 cm^2
31. 4 cm
32. 218.064 cm^3
33. Rs. 82720
34. 2.5 cm
35. 10
36. 5 cm, 3 cm
37. 770 cm^2
38. 1:2

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